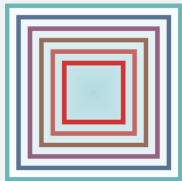


# Grid-aware Flexibility Aggregation for Zonal Balancing Markets

Efthymios Karangelos & Anthony Papavasiliou

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Athens, Greece.

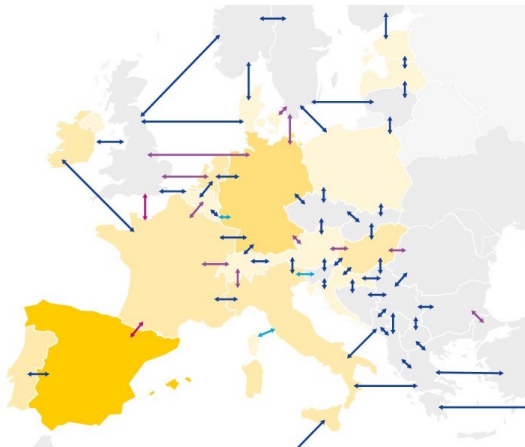
ICEBERG Interim Workshop,  
June 14, 2024,  
Athens, Greece



PSCC 2024

Efthymios Karangelos and Anthony Papavasiliou, "*Grid-aware Flexibility Aggregation for Zonal Balancing Markets*", Electric Power Systems Research (2024) – in press.

# Cross-border integration for electricity balancing



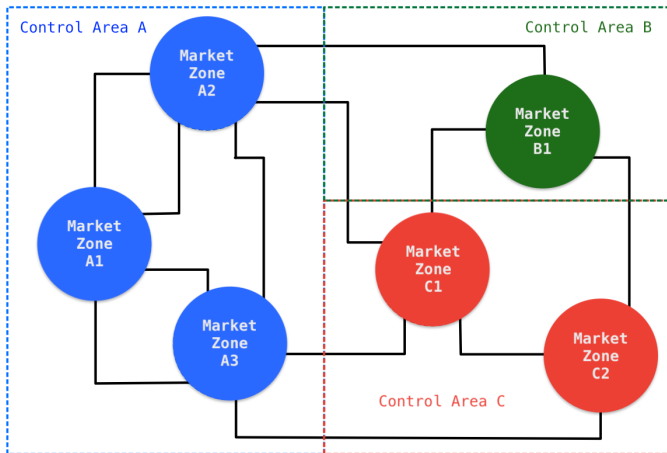
Source: ENTSO-e website



AI generated image

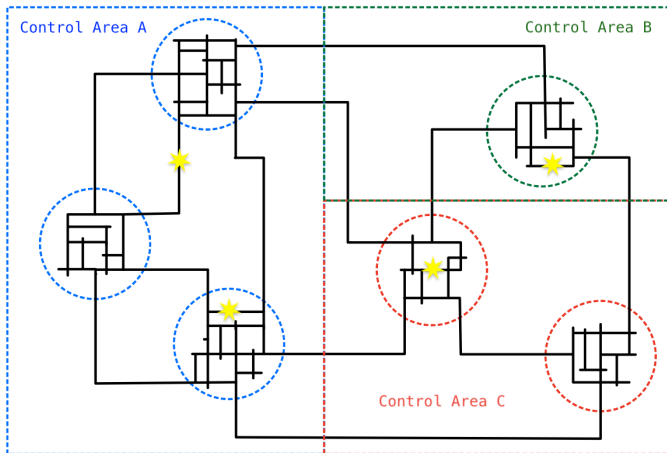
# How is the grid represented?

- Balancing market clears at the zonal resolution.



# How is the grid represented?

- Intra-area **congestion** to be managed by respective TSO.



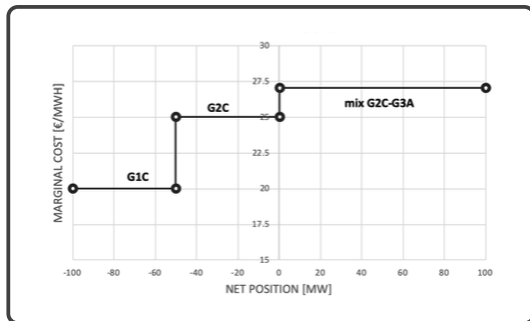
## *Ex-ante* Bid Filtering

- ▶ TSO can filter any intra-area bid that is anticipated to cause congestion.
  - ✗ How to do this?
  - ✗ Intra-zonal grid constraints hidden from the market?
  - ✗ TSO risk aversion also hidden from the market?

## *Ex-post* Bid Blocking

- ▶ TSO can block & replace any activated intra-area bid to resolve congestion.
  - ✗ Only replacing within the same zone causes inefficiencies?

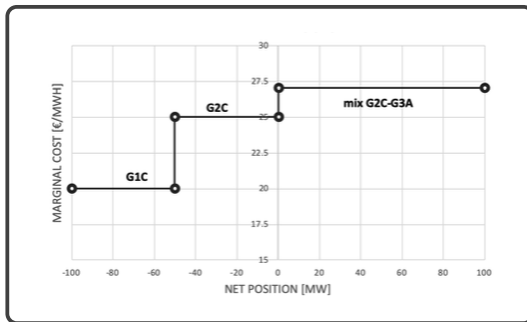
- ▶ Aggregate intra-zonal resources into a price – quantity curve (*ex-ante*).
  - ✓ Communicate both resource & intra-zonal congestion mgmt costs.



- ▶ Dispatch & settle intra-zonal resources s.t. grid constraints (*ex-post*).

# Residual Supply Function (RSF) *ex-ante* approximation

- ▶ Given an export volume, minimize intra-area cost s.t. grid constraints.
  - 🕒 over an export volume range:



- ▶ Resulting price – quantity curve can be submitted in the zonal market.



# Aggregation/disaggregation approach [1, 2, 3]

## Residual Supply Function (RSF) *ex-ante* approximation

- ▶ Given an export volume, minimize intra-area costs s.t. grid constraints.
  - ↳ to construct a price – quantity curve.

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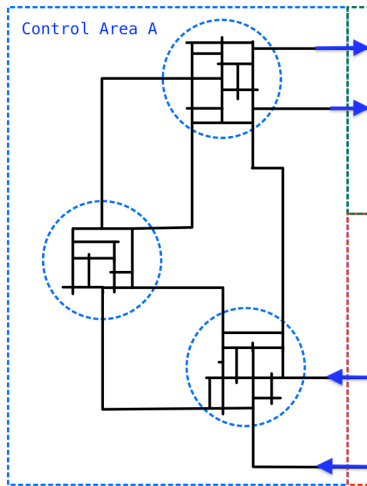
## Why revisit?

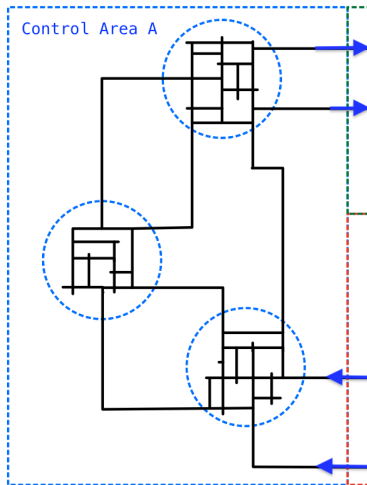
- ▶ Incremental export cost depends on uncertain & unobservable factors:
  - realization of imbalances all over the multi-area grid.
  - activation of balancing bids in external control-areas.
  - detailed topologies of external control-areas.
- ▶ Represented by a single “*best-guess*” in [2, 3]:
  - ★ comes with the **risk** that the **disaggregation cost** may be greater than approximated by the RSF (a.k.a., disaggregation risk).

# 1. Proposal

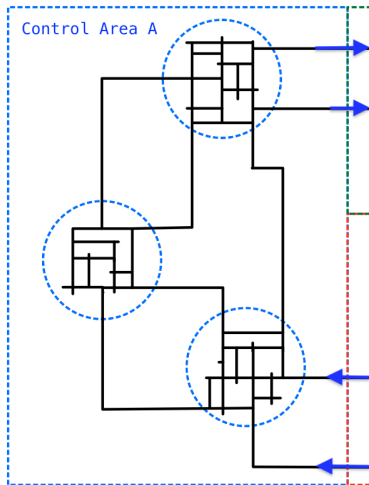
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# Introducing boundary injection changes



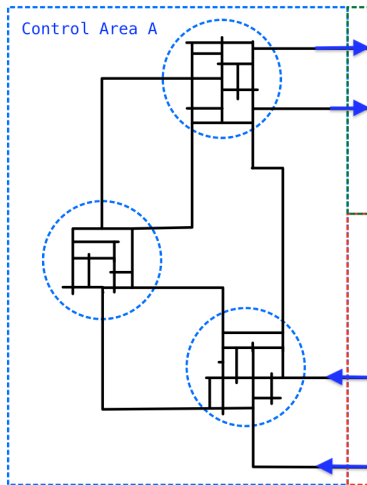


- ▶ The changes in the interconnector power flows, after the balancing market activations.
- ▶ For any given export volume:
  - depend on the unobservable state of external control-areas,
  - also on the precise location of the demand for balancing power,
  - translate into intra-area power flows,
  - also into the minimum cost of exporting the considered volume.
- ▶ We consider these a **proxy** of the external balancing demand.



## Worst-Case RSF approximation

- ▶ Assume a **range** of boundary injection changes, caused by the balancing market.
  - ▶ Given any export volume, compute the **upper bound** of the intra-area minimum export cost within this assumed range.
- 🕒 to construct a price – quantity curve.



## Worst-Case RSF approximation

- ▶ A larger (smaller) range of boundary injection changes implies...
  - a larger (smaller) upper bound on the intra-area minimum export cost,
  - a smaller (larger) disaggregation risk.
- ✓ WcRSF also communicates the disaggregation risk aversion with the balancing market.

## 2. Mathematical formulation & solution approach

---



# How to compute the WcRSF approximation?

For any market zone  $\bar{z}$  and export volume  $e_{\bar{z}}$

$\max \{ \text{Operating Cost}(\text{Zonal Flexibility}) \};$   
 $s.t.$   
 $\text{Boundary Injection Changes} \in \text{Plausible Range};$   
 $\min \{ \text{Operating Cost}(\text{Zonal Flexibility}) \};$   
 $s.t.$   
 $\text{Nodal Balance}(\text{Boundary Injection Changes}, \text{Zonal Flexibility});$   
 $\text{Zonal Flexibility} \in \text{Limits of Zonal Resources};$   
 $\text{Intra-area power flows} \in \text{Branch Capacity Limits}.$

- For any market zone  $\bar{z} \in \mathcal{Z}$

$\mathcal{N}_{a(\bar{z})}$ : nodes with interconnectors outside the respective control area.

$\phi_{nx}$ : is the boundary injection change towards external node  $x \in \mathcal{X}_n^{a(\bar{z})}$ .

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- For any given target export quantity  $e_{\bar{z}}$

$$\phi_{nx}^{\min} \leq \phi_{nx} \leq \phi_{nx}^{\max}, \quad \forall n \in \mathcal{N}_{a(\bar{z})}, x \in \mathcal{X}_n^{a(\bar{z})}, \quad \# \text{ lower/upper bounds} \quad (1)$$

$$\sum_{n \in \mathcal{N}_{a(\bar{z})}} \sum_{x \in \mathcal{X}_n^{a(\bar{z})}} \phi_{nx} = e_{\bar{z}}. \quad \# \text{ net change balances export quantity} \quad (2)$$

*N.b.:* definition of boundary injection bounds to be discussed ...

$$\min_{p, \theta, s} \sum_{b \in \mathcal{B}_{\bar{z}}} c_b \cdot p_b + \sum_{n \in \mathcal{N}_{a(\bar{z})}} pen \cdot (s_n^+ + s_n^-), \quad (3)$$

subject to:

$$\sum_{b \in \mathcal{B}_n} p_b = \sum_{j \in \mathcal{N}_n} \frac{\theta_n - \theta_j}{X_{nj}} + \sum_{x \in \mathcal{X}_n^{a(\bar{z})}} \phi_{nx} + (s_n^+ - s_n^-), \quad \forall n \in \mathcal{N}_{a(\bar{z})}, \quad (4)$$

$$p_b^{\min} \leq p_b \leq p_b^{\max}, \quad \forall b \in \mathcal{B}_{\bar{z}}, \quad (5)$$

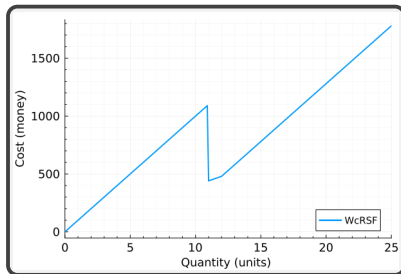
$$p_b = 0, \quad \forall b \in \mathcal{B}_z, \forall z \in \mathcal{Z} \setminus \bar{z} : a(z) = a(\bar{z}), \quad (6)$$

$$-\bar{f}_{nj} \leq \frac{\theta_n - \theta_j}{X_{nj}} + f_{nj}^0 \leq \bar{f}_{nj}, \quad \forall n, j \in \mathcal{N}_{a(\bar{z})} \quad (7)$$

$$s_n^+, s_n^- \geq 0, \quad \forall n \in \mathcal{N}_{a(\bar{z})}. \quad (8)$$

- ▶ *“The global maximum of a convex function over a closed bounded convex set is an extreme point.”*
  - The optimal value of the lower level (3–8) is piece-wise convex in the upper level decision variable.
  - ✓ The upper level maximizes a convex function in a closed bounded set (1–2).
- ▶ We can just exhaustively evaluate the lower level problem (3–8) over all corner points of (1–2):
  - the number of corner points depends on the number of interconnectors,
  - this is not prohibitively large for typical power grids,
  - it is also trivial to parallelize the solution of the respective linear programs.

- ▶ The Worst-Case resource aggregation cost (*i.e.*, the optimal value of the Bi-Level problem) is **non-convex in the target export quantity**.

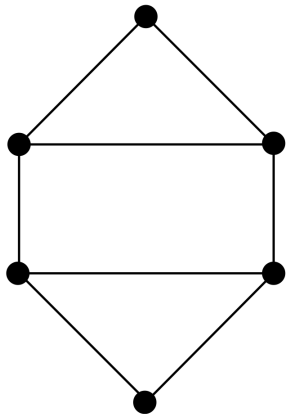


- ▶ In the PSCC paper, we added logical constraints in the balancing market clearing problem to represent price – quantity **ordered bids**.
- ▶ Since then, we also developed a translation into **exclusive block bids**.

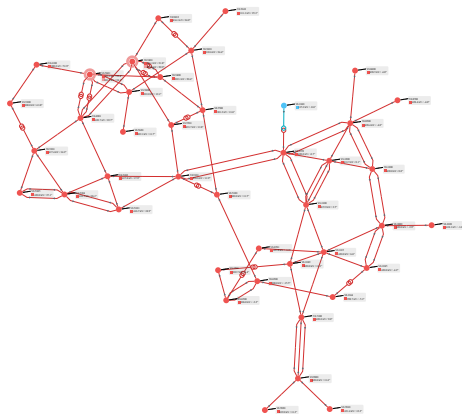
### 3. Results & discussion

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# The test systems



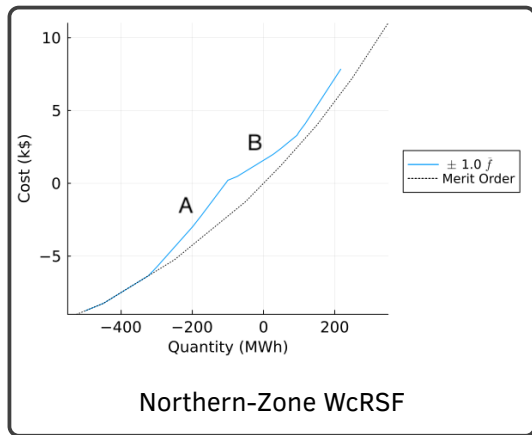
The Chao-Peck example



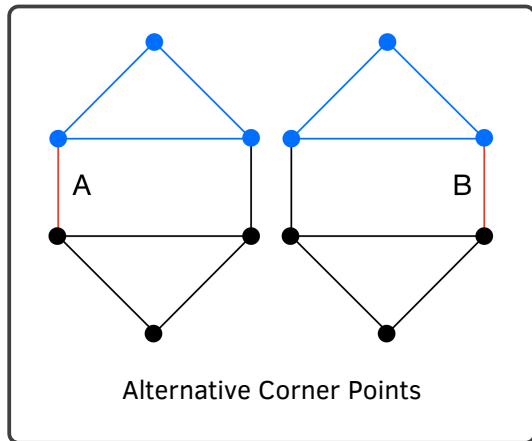
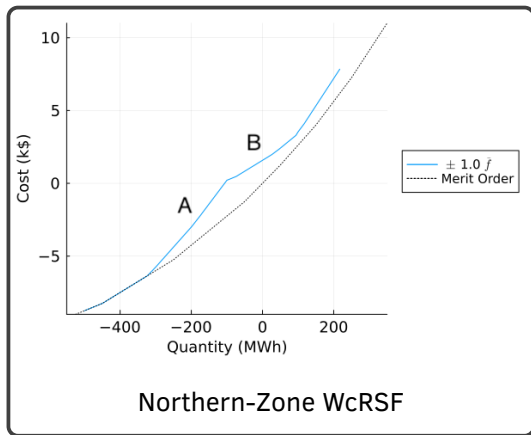
The Nordic System (N44 BC) case



# Chao-Peck example: intra-zonal resource aggregation



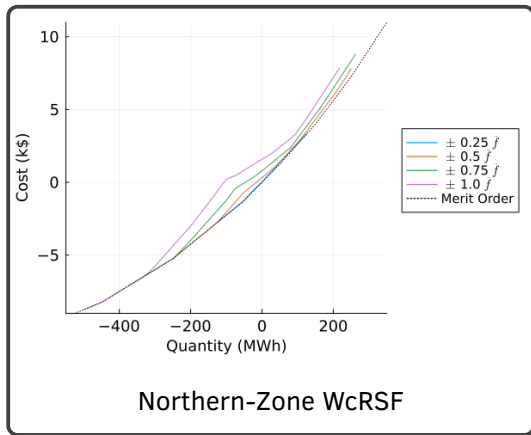
# Chao-Peck example: intra-zonal resource aggregation



**Too narrow:** WcRSF touches the resource cost curve (a.k.a. merit order).

**Too wide:** Sharing balancing resources looks infeasible!

**Just-right:** Recovering the eventual delivery cost for the Activated Quantity.



# How to evaluate the WcRSF?

The process (Q over 1000 samples):

- 0 Generate nodal imbalance sample.
  - 1 Clear Zonal Balancing Market given the WcRSF for a zone of study.
  - 2 Disaggregate Activated Balancing Quantity s.t. intra-area grid constrains.
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The metrics (average values):

- $Q_a$ : the Activated Balancing Quantity (in MWh).
- $CD_a$ : the Disaggregation Cost (in money).
- $CO_a$ : the Activated Offer Cost as per the aggregated offer (in money).
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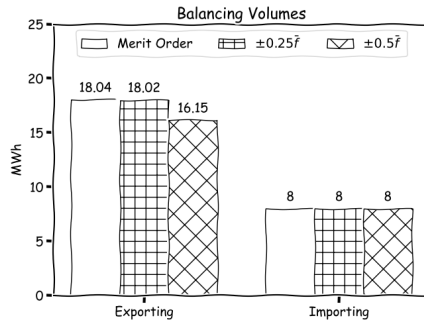
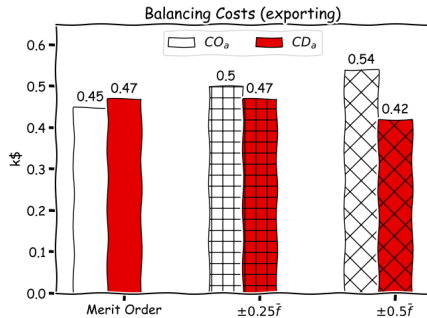
$CO_a$ : the Activated Offer Cost as per the aggregated offer (in money).

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**The alternative:** All bids from the zone of study sent to the market (merit order aggregation).

# Chao-Peck example – simulation results overview

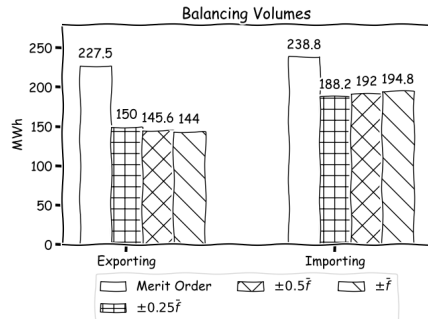
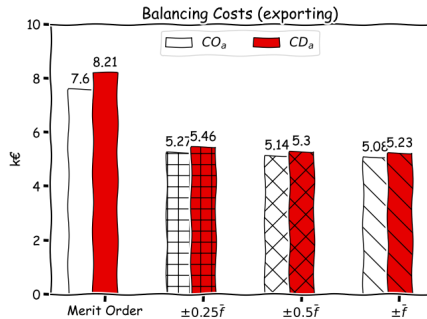
Average values over 1000 imbalance samples



- ▶ A moderate boundary injection range  $\pm 0.25\bar{f}$  sufficient to recover the disaggregation cost.
- ▶ Too much risk aversion reduces the competitiveness of the balancing resources.

# Nordic test case – simulation results overview

Average values over 1000 imbalance samples

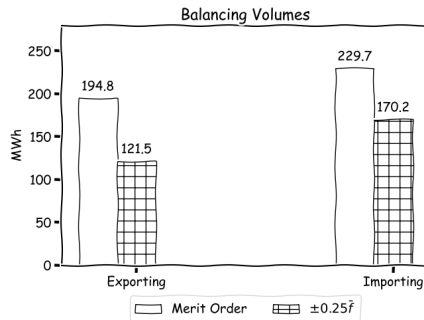
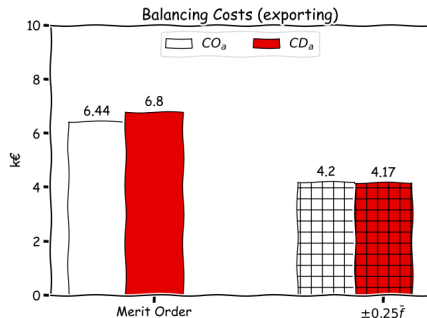


✗ Even at a very conservative range ( $\pm \bar{f}$ ) there is a negative gap between the average Disaggregation Cost and Aggregated Offer Cost!



# Modified Nordic test case

without imbalance realizations within aggregation area



- Grid congestion still possible while sharing balancing resources.
- ✓ the WcRSF hedges correctly against this risk.

- ▶ Flexibility resource aggregation in the context of zonal balancing markets.
- ▶ Proposal to evaluate the worst-case intra-area congestion cost over a plausible range of interconnection power flow changes.
- ▶ Purpose is to communicate intra-area grid constraints and congestion risk aversion with the market.

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- ▶ Proposal to evaluate the worst-case intra-area congestion cost over a plausible range of interconnection power flow changes.
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- ✓ Given a suitable range, hedging vs the risk of costly intra-area congestion.

- ▶ Flexibility resource aggregation in the context of zonal balancing markets.
- ▶ Proposal to evaluate the worst-case intra-area congestion cost over a plausible range of interconnection power flow changes.
- ▶ Purpose is to communicate intra-area grid constraints and congestion risk aversion with the market.
- ✓ **Given a suitable range, hedging vs the risk of costly intra-area congestion.**
  - further work on defining the range from historical data.
  - also on accounting for intra-area uncertainties.

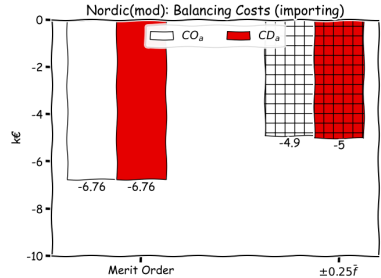
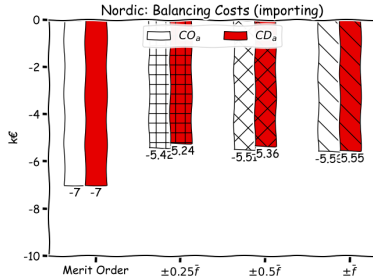
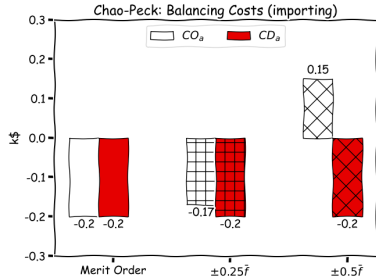


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# References

- [1] I. Mezghani, N. Stevens, A. Papavasiliou, and D. I. Chatzigiannis, “Hierarchical coordination of transmission and distribution system operations in European balancing markets,” IEEE Transactions on Power Systems, 2022.
- [2] A. Papavasiliou, M. Bjørndal, G. Doorman, and N. Stevens, “Hierarchical balancing in zonal markets,” in 2020 17th International Conference on the European Energy Market (EEM). IEEE, 2020, pp. 1–6.
- [3] A. Papavasiliou, G. Doorman, M. Bjørndal, Y. Langer, G. Leclercq, and P. Crucifix, “Interconnection of Norway to European balancing platforms using hierarchical balancing,” in 2022 18th International Conference on the European Energy Market (EEM), 2022, pp. 1–7.

# Case studies – results over importing samples



## Logical Constraints for Ordered (price, quantity) Bids

$$q_{k,z} = u_{k,z} \cdot dq_{k,z}^{\max} + dq_{k,z}, \quad \forall k \in \mathcal{K}_z, \forall z \in \mathcal{Z}_{\bar{a}}, \quad (9)$$

$$0 \leq dq_{k,z} \leq v_{k,z} \cdot dq_{k,z}^{\max}, \quad \forall k \in \mathcal{K}_z, \forall z \in \mathcal{Z}_{\bar{a}}, \quad (10)$$

$$v_{k,z} + u_{k,z} \leq u_{k-1,z}, \quad \forall k \in \mathcal{K}_z^+, \forall z \in \mathcal{Z}_{\bar{a}}, \quad (11)$$

$$v_{k,z} + u_{k,z} \leq u_{k+1,z}, \quad \forall k \in \mathcal{K}_z^-, \forall z \in \mathcal{Z}_{\bar{a}}, \quad (12)$$

$$\sum_{k \in \mathcal{K}_z} v_{k,z} \leq 1, \quad \forall z \in \mathcal{Z}_{\bar{a}}, \quad (13)$$

$$u_{-1,z} + u_{1,z} \leq 1, \quad \forall z \in \mathcal{Z}_{\bar{a}}, \quad (14)$$

$$v_{k,z}, u_{k,z} \in \{0; 1\}, \quad \forall k \in \mathcal{K}_z, z \in \mathcal{Z}_{\bar{a}}. \quad (15)$$